

1.– Find the area enclosed by the curves.

a) $y = x^{5/3}$; $x = 1$; $x = 8$; $y = 0$.

b) $y = 4x - x^2$; $y = 0$; $x = 1$; $x = 3$.

c) $x = 1 + y^2$; $x = 10$.

d) $y = 9 - x^2$; $y = x + 3$.

e) $y = x^2 - 4$; $y = 8 - 2x^2$.

f) $y = x^4 - 4x^2$; $y = 4x^2$.

g) $y = e^x$; $y = e^{-x}$; $x = 0$; $x = 2$.

h) $xy = 12$; $x = 0$; $y = 1$; $y = e^2$.

i) $y = \frac{1}{1+x^2}$; $y = 0$; $x = \pm 1$.

j) $y = 0$; $y = \tan x$; $x = 0$; $x = \pi/4$.

k) $y = \sqrt{x}$; $y = x^3$.

l) $y = x^{1/3}$; $y = x^2$.

2.– Find the following areas:

a) Interior to $\rho = \cos 4\theta$.

b) Interior to $\rho = 1 + \sin \theta$.

c) Interior to $\rho^2 = a^2 \cos 2\theta$.

d) Interior to $\rho = a \cos 3\theta$.

e) Interior to $\rho = 1 + \cos \theta$ and exterior to $\rho = 1$.

f) Common to $\rho = 3 \cos \theta$ and $\rho = 1 + \cos \theta$.

3.– Find the area enclosed by:

a) Axis $y = 0$ and the curve given in parametrics by $x = t - \sin t$; $y = 1 - \cos t$; $t \in [0, 2\pi]$.

b) The curve $x = 3 + \cos t$; $y = 4 \sin t$.

c) The curve in parametrics: $x = a \cos t$, $y = b \sin t$.

d) Axis OX and the curve $x = \sqrt{t}$, $y = \sqrt{t} \sin t$; $t \in [0, \pi]$.

e) The curves $y = 9 - x^2$; $64x = y^2$; $y = 2x^2$ on the first quadrant.

f) The curve $y^2 - x^2 + x^4 = 0$.